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Methodology to Evaluate Fatigue Damage of High-Speed Train Welded Bogie Frames Based on On-Track Dynamic Stress Test Data

Guangxue Yang^{1*}, Meng Wang², Qiang Li¹ and Ran Ding¹

Abstract

The current method of estimating the fatigue life of railway structures is to calculating the equivalent stress amplitude based on the measured stress data. However, the random of the measured data is not considered. In this paper, a new method was established to compute the equivalent stress amplitude to evaluate the fatigue damage based on the measurable randomness, since the equivalent stress is the key parameter for assessment of structure fatigue life and load derivation. The equivalent stress amplitude of a high-speed train welded bogie frame was found to obey normal distribution under uniform operation route that verified by on-track dynamic stress data, and the proposed model is, in effect, an improved version of the mathematical model used to calculate the equivalent stress amplitude. The data of a long-term, on-track dynamic stress test program was analyzed to find that the normal distribution parameters of equivalent stress amplitude values differ across different operation route. Thus, the fatigue damage of the high-speed train welded bogie frame can be evaluated by the proposed method if the running schedule of the train is known a priori. The results also showed that the equivalent stress amplitude of the region connected to the power system is more random than in other regions of the bogie frame.

Keywords: Fatigue damage evaluation, Equivalent stress amplitude, On-track dynamic stress test, Welded bogie frame of high-speed train

1 Introduction

Safety is the most important property of a passenger railway vehicle. The fatigue strength of a vehicle loading structure has a substantial impact on its safety, and thus must be comprehensively assured. A series of fatigue strength analysis methods for welded railway vehicle structures have been introduced to date [1], including fatigue assessment for constant amplitude loading by the endurance limit, evaluation of fatigue test programs by cumulative damage, and evaluation of simulated multiple body systems by cumulative damage. These methods are commonly applied in the railway industry [2-6].

Han et al. [7] introduced a static load test method and evaluated experimentally the static strength for the bogie

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bodies. As part of the Euraxles project, a series of fullscale axles fatigue tests were carried out [13]. The fatigue limits and the stress concentration factors were verified. However, most published research are not determined based on actual, on-track test programs of the structure in question.

The speed and efficiency of train travel has been continually modernized over recent decades, so the real load situation of vehicles may differ substantially from the standard. Furthermore, the vehicle structures may crack unexpectedly during the service period [14]. The load situation of railway vehicles have been researched recently. By use of a reliable test technology, Ren et al. [15] tested the axle spring forces of the high speed EMU on the Beijing-Tianjin railway line. Zhu et al. [16] carried out theoretical research and experimental validation to investigate load spectra of high-speed trains bogie frames. Wu et al. [17] investigated the post-derailment dynamic behavior of the half car and verified the proposed postderailment dynamic model.

The bogie frame is one of the most important parts of the railway vehicle [18–22]. It plays a significant role in controlling wheel sets on the railway, and it carries the brakes, motors, gear boxes, and suspensions while sustaining the static weight of the car body. To this effect, the load conditions of the bogie frame are highly complex and accurately assessing its fatigue strength is very challenging. Numerous welded structures of railway vehicles are safety critical [23, 24]. The dynamic stress on-track test, one of the most feasible and effective approaches to obtaining fatigue stress cycles [25], was utilized in this study on a long-term China high-speed train program to explore the dynamic stress response of the bogie frame. The results were used to build a new method for evaluating the on-track fatigue damage of the bogie frame.

2 Dynamic Stress Test Program

Figure 1 shows the dynamic stress test point distribution of the China high-speed train bogie frame. The strain gauge is disposed at the junction of the weld metal and the base metal, as shown in Figure 2. The tested vehicle was still in service on several railway lines including Beijing West-Guangzhou South, Beijing West-Taiyuan-Guangzhou South, and others throughout the duration of the dynamic stress test program.

The bogie frame was subjected to a combined, multilevel stress during train operation. To facilitate followup analysis, the multi-level stress was transformed into equivalent constant amplitude stress based on the fatigue damage consistency law. In other words, equivalent stress is the most important parameter for fatigue.

According to the rules of the rain flow count method, the stress spectrum must first be obtained from the test data



before calculating the fatigue damage under Miner damage accumulation theory based on the stress spectrum. The tested fatigue damage D_1 , according to the tested miles L_1 (km), is:

$$D_1 = \sum_{i=1}^{a} \frac{n_i}{N_i} + \sum_{j=1}^{b} \frac{n_j}{N_j} = \sum_{i=1}^{a} \frac{n_i \sigma_i^{m_1}}{C_1} + \sum_{j=1}^{b} \frac{n_j \sigma_j^{m_2}}{C_2},$$
(1)

S-N curve parameters can be determined based on Ref. [26].

The fatigue damage of equivalent stress $\sigma_{\rm e}$ after 2×10^6 cycles is denoted as *D*. The following equation makes *D* equal to the total fatigue damage of the train according to the whole service life miles *L* (km):

$$D = \frac{N\sigma_e^{m_1}}{C_1}.$$
(2)



On the basis of the fatigue damage consistency law, tested damage D_1 should be equal to the entire damage D per kilometer:

$$\frac{D}{L} = \frac{D_1}{L_1}.$$
(3)

Eq. (3) can be written as a stress-type equation:

$$\frac{N\sigma_e^{m_1}}{C_1L} = \sum_{i=1}^a \frac{n_i \sigma_i^{m_1}}{C_1L_1} + \sum_{j=1}^b \frac{n_j \sigma_j^{m_2}}{C_2L_1},\tag{4}$$

where

$$\sigma_e = \left(\frac{L}{L_1 N} \sum_{i=1}^{a} n_i \sigma_i^{m_1} + \frac{L C_1}{L_1 C_2 N} \sum_{j=1}^{b} n_j \sigma_j^{m_2}\right)^{1/m_1}.$$
(5)

Engineers often utilize the linear S-N curve to ensure structural safety [27]. Let $C_2 = C_1$, $m_2 = m_1$ so that Eq. (5) becomes:

$$\sigma_e = \left(\frac{L}{L_1 N} \sum_{k=1}^{a+b} n_k \sigma_k^{m_1}\right)^{1/m_1}.$$
(6)

Eq. (6) is the equivalent stress amplitude calculation formula based on the measured data. L equals 12 million km, according to the known high-speed train service life.

The dynamic stress responses of the bogie frame were obtained by the test program as the train ran on the Taiyuan-Guangzhou South line. The equivalent stress amplitudes according to Eq. (6) of each tested stress point are shown in Table 1.

A long-term tracking dynamic stress test was conducted on a passenger-carrying operation train with regular maintenance on common tracks, which represent the normal level. The equivalent stress amplitudes of D10 and D11

Table 1	Equivalent	t stress	values	of	the	frame
under u	iniform ope	ration (MP	a)			

Test points	Test data and	m)	
	8.1.2013 262,644	8.3.2013 267,679	8.9.2013 277,979
D04	54.9	52.8	56.6
D09	72.6	70.6	73.0
D10	67.1	65.4	67.9
D11	67.4	65.4	68.3
D12	58.8	57.5	59.2
D15	51.0	48.2	51.7
D16	43.6	42.6	44.3
D18	54.8	54.0	55.9
D21	51.0	50.1	52.3
D22	48.0	46.8	48.8
D23	45.4	46.5	47.9
D24	85.8	81.2	87.2

Note: Due to the confidentiality requirements of the project, the equivalent stress amplitude data in the table is uniformly superimposed with an identical random number. Equivalent stress amplitude data presented below were processed in the same manner

along with the operating mileage from 18.5 $\times ~10^4$ km to 95.7 $\times ~10^4$ km are shown in Figures 3 and 4.

3 Methodology

If the whole service miles of bogie frame is cut into *x* pieces, the fatigue damage of each piece can be calculated as follows:

$$D_{i=1,2...x} = \frac{(\sigma_e)_i^{m_1} N}{C_1} \frac{L_i}{L}.$$
(7)

The whole fatigue damage of the bogie frame in total service miles is:

$$D = \sum_{i=1}^{x} D_i = \sum_{i=1}^{x} \left[\frac{(\sigma_e)_i^{m_1} N}{C_1} \frac{L_i}{L} \right].$$
 (8)

Because the ratio between test miles L_1 and whole service miles L is the probability of each equivalent stress amplitude tested, Eq. (8) can be rewritten as follows:

$$D = \sum_{i=1}^{x} \left[\frac{(\sigma_e)_i^{m_1} N}{C_1} \cdot p(\sigma_e)_i \right]$$

= $\frac{N}{C_1} \sum_{i=1}^{x} \left[(\sigma_e)_i^{m_1} p(\sigma_e)_i \right].$ (9)

As the piece number x increases towards infinity, Eq. (9) can be rewritten in integral form:





$$D = \lim_{x \to \infty} \frac{N}{C_1} \sum_{i=1}^{x} \left[(\sigma_e)_i^{m_1} p(\sigma_e)_i \right]$$

= $\frac{N}{C_1} \int \left[(\sigma_e)_i^{m_1} p(\sigma_e)_i \right] \mathbf{d}(\sigma_e)_i.$ (10)

The following equation makes $[\sigma_e]$ equal to the damage consistency equivalent stress amplitude according to the entire service mileage of the bogie frame:

$$([\sigma_e])^{m_1} = \int \left[(\sigma_e)_i^{m_1} p(\sigma_e)_i \right] \mathsf{d}(\sigma_e)_i, \tag{11}$$

where the key to acquiring the damage consistency equivalent stress amplitude is in determining the probability distribution of tested equivalent stress amplitude.

4 Application and Discussion

By comparison between Figures 3 and 4, the equivalent stress amplitudes of D11 were selected to determine the probability distribution of tested equivalent stress amplitude on account of their randomness. Table 2 shows the tested equivalent stress amplitude values of D11 in different operation routes according to the information shown in Figure 4.

Due to the regular maintenance of railway lines and rail vehicles, the running performance of rail vehicles is relatively stable. It is reasonable to suppose that deviations among the tested equivalent stress amplitudes are caused by stochastic factors when running conditions are constant. The tested equivalent stress amplitudes can be written in the following form according to the error analysis theory:

$$\sigma_e = \sigma + \varepsilon(0, s^2). \tag{12}$$

Predictably, the equivalent stress amplitude is in normal distribution $N(\sigma, s^2)$, so the whole service life fatigue damage of the bogie frame can be calculated as following formula under the " 3σ Principle":

$$D = \frac{N}{C_1} \int_{\sigma-3s}^{\sigma+3s} (\sigma_e)^{m_1} \cdot \frac{1}{\sqrt{2\pi s}} e^{-\frac{(\sigma_e-\sigma)^2}{2s^2}} \mathsf{d}(\sigma_e).$$
(13)

Because the tested equivalent stress amplitude belongs to a small sample size, the Anderson–Darling test method was used to test whether the equivalent stress amplitude followed a normal distribution. The test statistic AD value can be determined as follows:

$$A^{2} = -n - \frac{1}{n} \sum_{i=1}^{n} (2i - 1)(\ln F(X_{i}) + \ln (1 - F(X_{n+1-i}))).$$
(14)

Small *A* value indicates that the tested equivalent stress amplitude obeys normal distribution. Normal distribution test conclusions are reflected by *P*-values, which can be acquired as follows:

$$A^{\prime 2} = A^2 \times \left(1 + \frac{0.75}{n} + \frac{2.25}{n^2}\right).$$
 (15)

When $13 > A'^2 > 0.600$,

$$P = \exp\left(0.9177 - 4.279 \times A^{\prime 2} - 1.38 \times \left(A^{\prime 2}\right)^2\right).$$
(16)

When $0.600 > A'^2 > 0.340$,

$$P = \exp\left(0.9177 - 4.279 \times A^{\prime 2} - 1.38 \times \left(A^{\prime 2}\right)^2\right).$$
(17)

No.	Running railway lines	Running railway lines						
	Beijing West-Guangzhou South	Guangzhou South- Beijing west	Guangzhou South- Taiyuan	Taiyuan-Guangzhou South	Beijing West- Taiyuan- Guangzhou South			
1	66.9	64.2	66.4	67.4	65.6			
2	67.9	61.2	63.1	65.4	64.3			
3	66.5	62.3	61.8	68.3	68.6			
4	67.2	62.5	62.3	64.8				
5	65.5	62.8	61.3	65.4				
6	64.8	61.7	60.3	64.6				
7	66.0	65.1		63.3				
8	65.8	62.6						
9	65.4	61.4						
10	64.7							
11	64.4							
12	64.0							
13	66.0							

Table 2 Tested equivalent stress values of D11 in different railway tracks (MPa)

Table 3 Normal test result of D11 testing point by Anderson-Darling test method

Item	Running railway lines						
	Beijing West- Guangzhou South	Guangzhou South- Beijing West	Guangzhou South- Taiyuan	Taiyuan-Guangzhou South	Beijing West- Taiyuan- Guangzhou South		
Sample size	13	9	6	7	3		
AD value	0.14	0.40	0.38	0.32	0.25		
Mean value	65.78	62.64	62.53	65.60	66.17		
Standard deviation	1.15	1.28	2.12	1.71	2.21		
P value	0.96	0.28	0.28	0.42	0.43		

When $0.340 > A'^2 > 0.200$,

$$P = \exp\left(-8.318 + 42.796 \times A^{\prime 2} - 59.938 \times \left(A^{\prime 2}\right)^2\right).$$
(18)

When $A'^2 < 0.200$,

$$P = \exp\left(-13.436 + 101.14 \times A^{\prime 2} - 223.73 \times \left(A^{\prime 2}\right)^2\right).$$
(19)

When the confidence coefficient is 95%, the assumption that tested equivalent stress amplitude closely obeys a normal distribution should be rejected if P < 0.05. The data shown in Table 2 was tested by Anderson–Darling test method to obtain the results shown in Table 3; said data does indeed follow normal distribution.

Table 4 shows the damage consistency equivalent stress amplitude of each railway line, which corresponds to fatigue damage, calculated by the method introduced in

Table 4 Damage consistency equivalent stress amplitude of each railway line (MPa)

Beijing West- Guangzhou South	Guangzhou South- Beijing West	Guangzhou South- Taiyuan	Taiyuan- Guangzhou South	Beijing West- Taiyuan- Guangzhou South
65.74	62.61	62.54	65.58	66.18

Section 3. Different railway lines exhibited different fatigue damage values, even on twin lines (e.g., Beijing West-Guangzhou South versus Guangzhou South-Beijing West). To compute the fatigue damage of the bogie frame as accurately as possible over the entire service life, both the damage consistency equivalent stress amplitude of each railway line train running and the operation schedule of the train are needed. These values allow the whole service life fatigue damage of the bogie frame to be calculated as follows:

$$D = \frac{N}{C_1} \sum_{i=1}^{a} [\sigma_e]_i^{m_1} p_i.$$
 (20)

The complex load conditions of the bogie frame create different stress responses across different locations on the frame, so the mean value are also disparate. The difference between the standard deviations merit further research. The data in Table 1 was transformed into a new sample group to analyze the distributed standard deviation parameters as follows:

$$(\sigma'_e)_{ij} = (\sigma_e)_{ij} - \frac{1}{j} \sum_{j=1}^n (\sigma_e)_{ij}.$$
 (21)

The standard deviation parameters of the testing points are relatively uniform if the new sample group can be represented by a normal distribution. The Anderson–Darling normality test results are shown in Table 5, where the new sample can be considered to have a significant normal distribution. The estimated distribution parameters of each bogie frame testing point are shown in Table 6, where no standard deviations exceed 3 except the D24 testing point, which is slightly greater than 3; point D24 is located in the connection region of the frame and power device gear-box.

Based on the above analysis, the equivalent stress amplitude of the frame can be represented by a normal distribution within 12 million km and the standard deviation is generally 3 or less. To make the integral part of Eq. (13)equal *G*, *G* is expressed as follows:

$$G = \int_{\sigma-3s}^{\sigma+3s} (\sigma_e)^{m_1} \cdot \frac{1}{\sqrt{2\pi s}} e^{-\frac{(\sigma_e-\sigma)^2}{2s^2}} \mathsf{d}(\sigma_e).$$
(22)

G value reflects the fatigue damage of the bogie frame. Its value was consistently calculated to be under the mean value 10–90 MPa, with standard deviation of 0.5–3 (Figure 5). Its projection along standard deviation direction is shown in Figure 6, where the width of the data line represents the impact of standard deviation to the *G* value.

The small range of the standard deviation indicates that fatigue damage is mainly affected by the mean value. Therefore, an accurate mean value estimate of equivalent stress amplitude distribution is an essential component of the on-track dynamic stress fatigue test program.

Table 5 Normaltestresultofnewsamplegroupby Anderson–Darling method

Sample size	AD value	Mean value	Standard deviation	P value
36	0.57	5.67×10 ⁻¹⁶	1.28	0.13

Table 6 Estimated distribution parameters of each bogieframe testing point

Test point	Mean value	Standard deviation
D04	54.77	1.90
D09	72.07	1.29
D10	66.80	1.28
D11	67.03	1.48
D12	58.50	0.89
D15	50.30	1.85
D16	43.50	0.85
D18	54.90	0.95
D21	51.13	1.11
D22	47.87	1.01
D23	46.60	1.25
D24	84.73	3.14





5 Conclusions

Studies have shown that high-speed train bogie frame fatigue damage contains randomness though in the same operation route. The evaluation method proposed in this paper can be adapted to accurately assess the fatigue damage of the bogie frame. Several characteristics of the fatigue damage to the bogie frame were identified here by analyzing actual dynamic stress testing data.

- (1) The equivalent stress amplitude on behalf of the bogie frame fatigue damage can be obtained by integral based on normal distribution and 3σ Principle, especially when conditions are constant. The mean value of distribution parameters is dependent on the specific location of the test point; the standard deviation maximum value is about 3. Standard deviation does not significantly affect fatigue damage, but mean value has a great effect on it, so the mean value evaluation accuracy should be the primary focus in establishing the test program.
- (2) Bogie frame fatigue damage differs when the train runs on different operation routes, even across twin lines. When the damage consistency equivalent stress amplitude of each running railway line and the operation schedule of the train are known a priori, the whole service life fatigue damage of the bogie frame can be calculated precisely. Fatigue damage varies across specific locations on the frame, but the dynamic stress responses of the region connected to the power system are generally more random than the responses in other regions.

Authors' Contributions

GY wrote the manuscript; QL was in charge of the whole trial; MW assisted with data analyses; RD assisted with the theoretical analysis. All authors read and approved the final manuscript.

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Competing Interests

The authors declare that they have no competing interests.

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